

# Laplace Transform Pairs

Function	Transform
$\delta(t)$	1
$\delta(t-\tau)$	$e^{-s\tau}$
1 or $u(t)$	$\frac{1}{s}$
$u(t-\tau)$	$\frac{1}{s}e^{-s\tau}$
$u(t) - u(t-\tau)$	$\frac{1}{s}(1 - e^{-\tau s})$
$e^{-at}u(t)$	$\frac{1}{s+a}$
$\frac{1}{a}(1 - e^{-at})u(t)$	$\frac{1}{s(s+a)}$
$\frac{1}{a-b}(e^{at} - e^{bt})u(t)$	$\frac{1}{(s-a)(s-b)}$
$\frac{1}{a-b}(ae^{at} - be^{bt})u(t)$	$\frac{s}{(s-a)(s-b)}$
$e^{-a(t-\tau)}u(t-\tau)$	$\frac{1}{s+a}e^{-s\tau}$
t or $tu(t)$	$\frac{1}{s^2}$
$(t-\tau)u(t-\tau)$	$\frac{1}{s^2}e^{-s\tau}$
$t^2u(t)$	$\frac{2}{s^3}$
$t^n e^{at}u(t)$	$\frac{n!}{(s-a)^{n+1}}$
$te^{-at}u(t)$	$\frac{1}{(s+a)^2}$

$t^2 e^{-at} u(t)$	$\frac{2}{(s+a)^3}$
$t^{n-1} e^{-at} u(t)$	$\frac{(n-1)!}{(s+a)^n}$
$\sin(\omega_0 t) u(t)$	$\frac{\omega_0}{s^2 + \omega_0^2}$
$\sin(\omega_0 t + \theta) u(t)$	$\frac{s \sin \theta + \omega_0 \cos \theta}{s^2 + \omega_0^2}$
$\cos(\omega_0 t) u(t)$	$\frac{s}{s^2 + \omega_0^2}$
$\cos(\omega_0 t + \theta) u(t)$	$\frac{s \cos \theta - \omega_0 \sin \theta}{s^2 + \omega_0^2}$
$e^{-at} \sin(\omega_0 t) u(t)$	$\frac{\omega_0}{(s+a)^2 + \omega_0^2}$
$e^{-at} \cos(\omega_0 t) u(t)$	$\frac{s+a}{(s+a)^2 + \omega_0^2}$
$2e^{-at} \cos(bt - \theta) u(t)$	$\frac{e^{j\theta}}{(s+a) + jb} + \frac{e^{-j\theta}}{(s+a) - jb}$
$e^{-at} \cos(bt - \theta) u(t)$	$\frac{(s+a)\cos \theta + b \sin \theta}{(s+a)^2 + b^2}$
$\frac{2t^{n-1}}{(n-1)!} e^{-at} \cos(bt - \theta) u(t)$	$\frac{e^{j\theta}}{\lceil (s+a) + jb \rceil^n} + \frac{e^{-j\theta}}{\lceil (s+a) - jb \rceil^n}$